

**P2** Known-plaintext attack

→ 7-letters known

→ For all unknown possible  $26!$

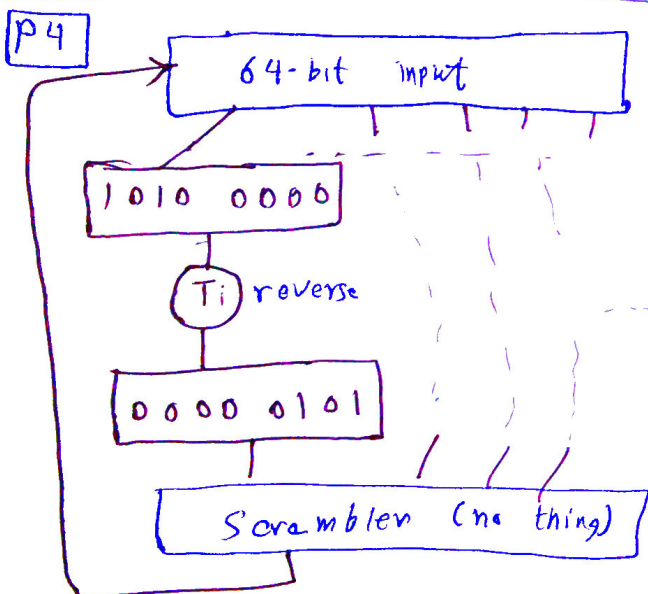
→ For 7 letters known

$$(26-7)! = 19!$$

We reduce possibility by

$$26! - 19! = 10^9$$

**P3** Yes, It's possible to know the key of cipher 1,2 (shift)



(a) result after  $n=3$

$$[0000 \ 0101][0000 \ 0101] \dots$$

(b) the input

$$[1010 \ 0000] \dots 1010 \ 0000$$

the result

$$[0000 \ 0101] \dots 1000 \ 0101$$

(c) Scrambler also reverse order

Step 1

الى بين القوسين  
هو الجزء المتكرر

before Scrambler

$$[0000 \ 0101] \dots 1000 \ 0101$$

after

$$1010 \ 0001 \dots [1010 \ 0000]$$

Step 2

before Scrambler

$$1000 \ 0101 \dots [0000 \ 0101]$$

after

$$[1010 \ 0000] \dots 1010 \ 0001$$

Step 3

before

$$[0000 \ 0101] \dots 1000 \ 0101$$

after

$$1010 \ 0001 \dots [1010 \ 0000]$$

**P6** (a)  $\begin{matrix} 100 & 100 & 100 \\ 011 & 011 & 011 \end{matrix}$

(b) she can know the pattern

$$(c) m(1) = 100$$

$$m(2) = 100$$

$$m(3) = 100$$

$$\rightarrow IV = c(0) = 111$$

$$\begin{aligned} \rightarrow c(1) &= K_S(c(0) \oplus m(1)) \\ &= K_S(011) = 100 \end{aligned}$$

$$\begin{aligned} \rightarrow c(2) &= K_S(c(1) \oplus m(2)) \\ &= K_S(000) = 110 \end{aligned}$$

$$\begin{aligned} \rightarrow c(3) &= K_S(c(2) \oplus m(3)) \\ &= K_S(010) = 101 \end{aligned}$$

$$m = 100 \ 100 \ 100$$

$$c = 100 \ 110 \ 101$$

**P7**  $p=3$   $q=11$

①  $n = p \cdot q = 33$

$z = (p-1)(q-1) = 20$

②  $e < n$   $e \rightarrow$  has no common factor with  $z$

$20 \rightarrow 20 \ 10 \ 5 \ 4 \ 2$

$e = 9 \rightarrow$  we choose this

$e \cdot d \ \% \ z = 1$

$d = ??$

$9 \cdot d \ \% \ 20 = 1$

$9 \cdot 9 \ \% \ 20 = 1$

$d = 9$

③  $C = m^e \ \% \ n$

'd'  $\rightarrow m=4 \rightarrow C = 4^9 \% 33$

'o'  $\rightarrow m=13 \rightarrow C = 13^9 \% 33$

'g'  $\rightarrow m=7 \rightarrow C = 7^9 \% 33$

④  $m = C^d \% n$

**P9**  $T_A = g^{S_A} \% P$

$T_B = g^{S_B} \% P$

$S = T_B^{S_A} \% P$

$S' = T_A^{S_B} \% P$

Prove that they are equal

$S = [g^{S_B} \% P]^{S_A} \% P$

$= g^{S_A S_B} \% P$

$= [g^{S_A} \% P]^{S_B} \% P$

$= T_A^{S_B} \% P = S'$